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Reconciling New Orleans Pumping Data with Gauge Observations of Isolated Extreme Rainfall
Due to Hurricane Isaac

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29 **ABSTRACT**

30 Slow-moving Hurricane Isaac affected the northern gulf coast between August 28th and
31 August 31st, 2012. Previous studies of the event reported on the hydrometeorology of the event
32 across southeast Louisiana and southern Mississippi (Lincoln, et al., 2013). This report provides
33 an in-depth examination and analysis of a suspected rainfall extreme in the New Orleans,
34 Louisiana metropolitan area. Event analysis for most natural watersheds involves examination of
35 river discharge data and the modeling of infiltration to infer watershed-average rainfall. New
36 Orleans is unique because its topography does not allow for runoff and rainfall must be pumped
37 out of the city. A methodology is proposed which uses data from pumping records as a proxy for
38 streamflow out of the New Orleans “watershed.” A hydrologic model was created estimate
39 runoff by modeling infiltration using the Green & Ampt method. Modeled runoff was compared
40 to runoff inferred from pumping records to validate rainfall estimates. Modeled runoff was
41 within 1% of the runoff inferred from pumping records; this strongly suggests that a relatively
42 extreme amount of rain – exceeding the 1% annual event – did occur over parts of New Orleans
43 during Hurricane Isaac.

44

45 **1. Introduction**

46 In “2012 Southeast Louisiana and Southern Mississippi Flooding Due to Hurricane
47 Isaac” (Lincoln, et al., 2013), preliminary data was presented for an isolated area of extreme
48 rainfall (greater than 20 inches) that occurred across a portion of the New Orleans metropolitan
49 area. Since the writing of that report, additional data was obtained and analyzed by hydrologists
50 at the National Weather Service (NWS) Lower Mississippi River Forecast Center (LMRFC).
51 Additional data included pumping records from the Sewerage and Water Board of New Orleans
52 (SWBNO). Some additional quality control work was also done to rain gauge data in the New
53 Orleans vicinity. This report is intended to supersede some data and conclusions regarding local
54 rainfall amounts in New Orleans found in Lincoln, et al. (2013), and is believed to be the most
55 comprehensive review of the local rainfall event currently available.

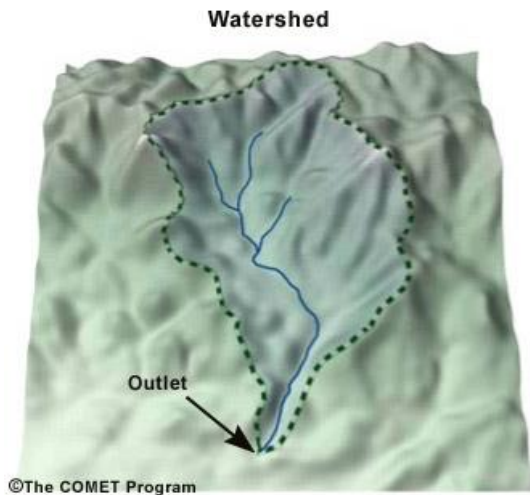
56 The following discussions consist of four subtopics: 1) The hydrology of New Orleans
57 and Hurricane Isaac’s impact; 2) estimating pumped flow rates; 3) further quality-control of
58 precipitation estimates (beyond that of Lincoln, et al (2013)) and modeling rainfall/runoff
59 relationships in portions of New Orleans during Isaac using a hydrologic model; and 4) the
60 results of our modeling analysis and comparing the results to observations.

61

62 *1a. New Orleans Hydrology*

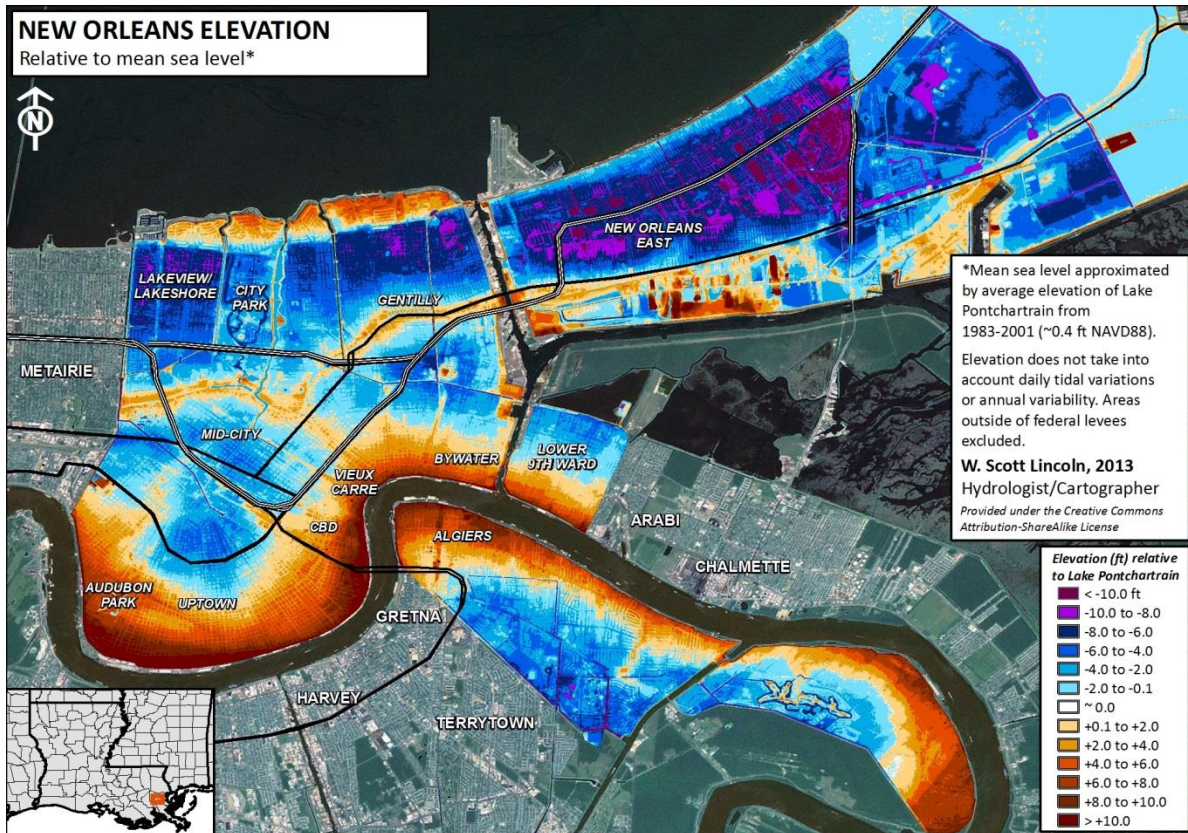
63 Most natural watersheds are defined by an outlet location that is typically the lowest
64 elevation in the watershed and ridges that separate the direction of overland flow toward the
65 outlet (Figure 1). Rainfall occurring in the typical watershed flows downhill from the higher
66 elevations into streams, and these streams then carry water to the outlet point where it leaves the
67 watershed. The city of New Orleans presents a unique hydrologic situation. New Orleans, in

68 contrast, is completely surrounded by higher terrain and rainfall would thus have a natural
69 tendency to collect in the lowest sections of the city unless otherwise removed by
70 evapotranspiration or pumping. A further complication is the fact that most of New Orleans
71 proper - about 65% - is at or below mean sea level (Figure 2), as defined by the average elevation
72 of Lake Pontchartrain during the 1983-2001 period, estimated at about 0.4 ft NAVD88.



74 Figure 1. A hypothetical watershed, as defined by the outlet point.

75



76

77 Figure 2. Elevation map of New Orleans excluding suburbs and areas outside of the federal
 78 levee system. Elevation is relative to mean sea level, as defined by Lake Pontchartrain average
 79 level from 1983-2001.

80

81 To facilitate drainage of stormwater out of New Orleans, the SWBNO operates 23
 82 pumping stations within the city, which contain 113 total pumps (Interagency Performance
 83 Evaluation Task Force, 2006). At a typical pumping station, storm water is either pumped from
 84 the underground storm sewer network into an outfall canal, or pumped from an outfall canal to
 85 Lake Pontchartrain. Since Hurricane Katrina, closure gates have been added to the outfall canals
 86 to prevent water in Lake Pontchartrain or Lake Borgne from entering the interior drainage
 87 system. Because of this, the United States Army Corps of Engineers (USACE) also operates

88 some pumping stations to move water from the interior drainage network out of the city.

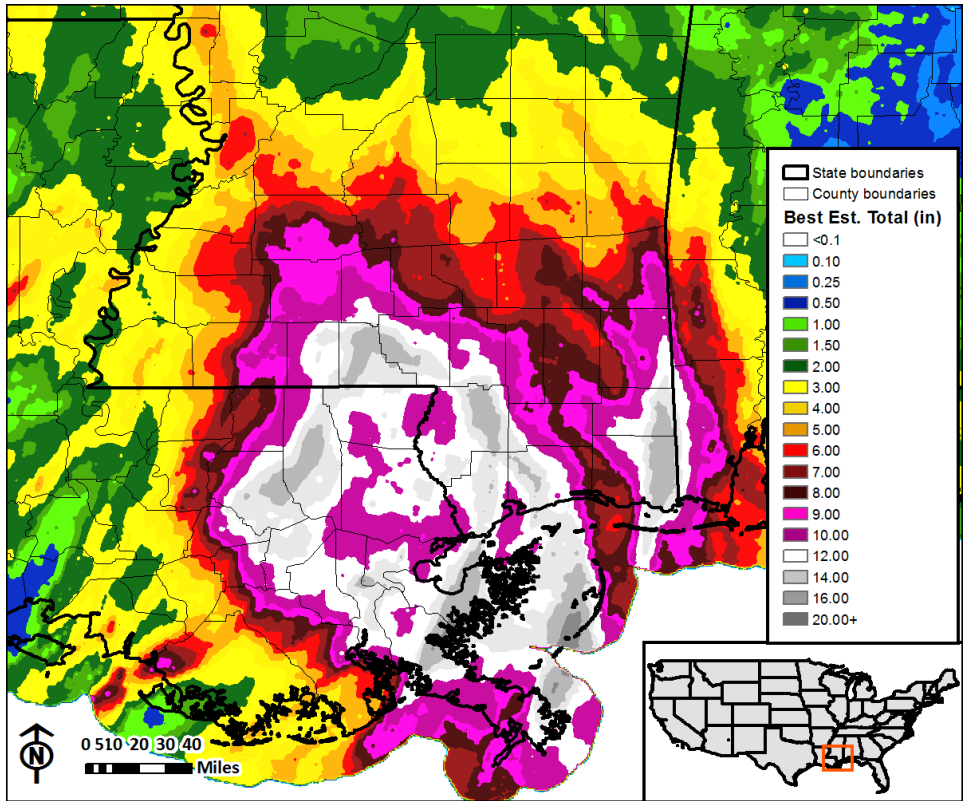
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90 *1b. Hurricane Isaac's effect on New Orleans*

91 As mentioned in “Appendix C” of Lincoln et al. (2013), an isolated area of very heavy
92 rainfall was observed in a small section of New Orleans (Figure 3). Two storm total rainfall
93 observations of over 20.0 inches in the Audubon Park vicinity of New Orleans were originally
94 considered questionable by NWS forecasters due to the lack of corroborating gauges nearby and
95 the lack of flooding reports in the area (anecdotally, “that much rain always causes flooding”).
96 Additional rainfall data was obtained after the storm, including rainfall from CoCoRaHS gauges
97 and from private weather stations. NWS forecasters also visited a few of these private gauges to
98 gather more information about potential sources of uncertainty. With five (5) gauges reporting
99 similar rainfall rates and rainfall accumulations near the Mississippi River – both in New Orleans
100 and close suburbs - Lincoln, et al. (2013) concluded that the questionable rainfall reports were
101 likely validated. It was also suggested that to further verify the rainfall amounts, pumping
102 records from the SWBNO could be evaluated because the pumped volume of water versus time
103 could serve as a proxy for streamflow measurement associated with a typical watershed. Here
104 we present findings from these additional efforts to verify the rainfall amounts in New Orleans.

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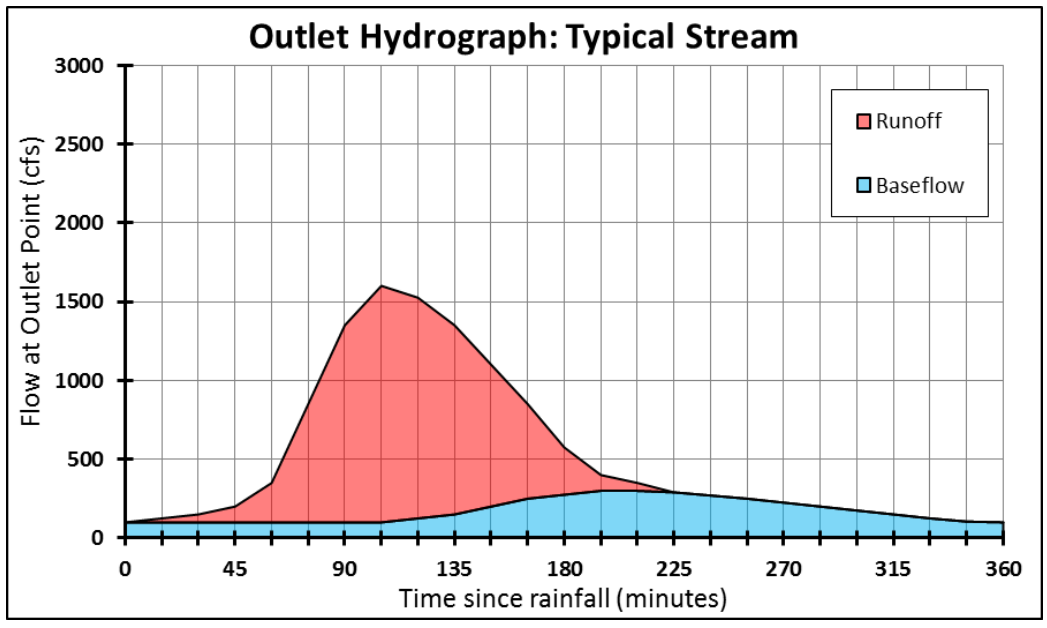
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108 Figure 3. Hurricane Isaac storm total rainfall as estimated by a combination of official gauges,
 109 radar data, and forecaster experience in the NWS RFC Best-Estimate product. Note swaths of
 110 higher rainfall in coastal Mississippi and southeast Louisiana, including the small, isolated
 111 maxima in the New Orleans area. Figure from Lincoln et al. (2013).

112 **2. Methodology**

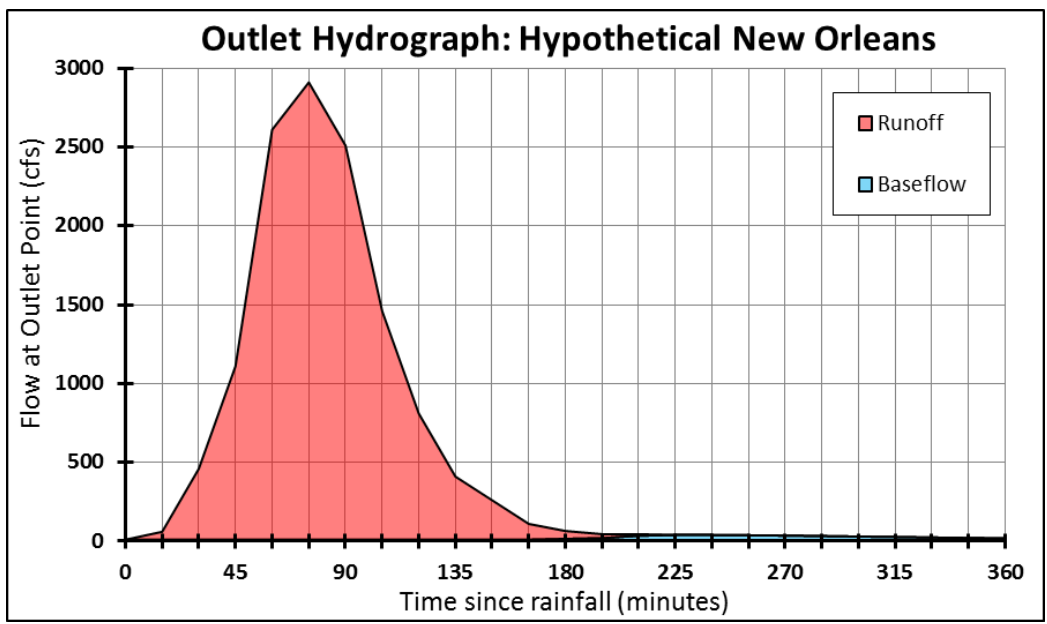
113 For natural watersheds, hydrologists can estimate the average runoff that occurred in the
114 watershed using stream observations at the outlet point. If a relationship between stream depth
115 and stream flow exists (called a rating curve), the total volume of water leaving a watershed
116 during an event can be estimated from the hydrograph (Figure 4). First, the baseflow
117 contribution is removed from the streamflow hydrograph. Then the rate of water leaving the
118 watershed at each timestep is summed and divided by the contributing area. The result is the
119 equivalent uniform depth (EDU), or average watershed runoff. The runoff can be described as
120 the portion of the rainfall that did not infiltrate into the soil, become intercepted by vegetation,
121 become trapped in detention areas, or evaporate. Thus, the runoff is a good estimate for the
122 minimum possible rainfall amount averaged across the watershed. Additional modeling
123 techniques can be used to estimate the total rainfall and total infiltration once the runoff is
124 known.

125 As mentioned earlier, the city of New Orleans does not behave like a typical watershed.
126 Because all rain that falls on the city of New Orleans must be pumped out, the volume of runoff
127 that occurred during an event could be approximated if the volume of water pumped is known or
128 can be reasonably estimated, similar to using the event runoff portion of a hydrograph in a
129 typical stream. A hypothetical hydrograph for the city of New Orleans would also differ from
130 that of a typical stream because the urban landscape would cause more rainfall to immediately
131 runoff to drainage canals and the storm sewer network due to impervious surfaces. This would
132 have the effect of greatly reducing the baseflow contribution, but increasing the runoff
133 contribution, making the hydrograph peak higher and quicker (Figure 5).



134

135 Figure 4. A hypothetical hydrograph for a typical stream’s watershed outlet point. Baseflow is
 136 the contribution from water stored in the soil below the water table that slowly moves toward
 137 streams in the watershed. Runoff is the direct contribution from rainfall that does not infiltrate
 138 into the soil but instead runs over the land surface to streams and then to the outlet point.
 139 Hydrologists can estimate the average runoff that occurred in a watershed by removing the
 140 baseflow contribution and integrating the remaining volume under the hydrograph.



141

142 Figure 5. A hypothetical hydrograph for the city of New Orleans’ watershed “outlet point.”
 143 Similar to Figure 4, but the urban landscape will cause much less baseflow and quicker,
 144 increased runoff, even for the same amount of rainfall.

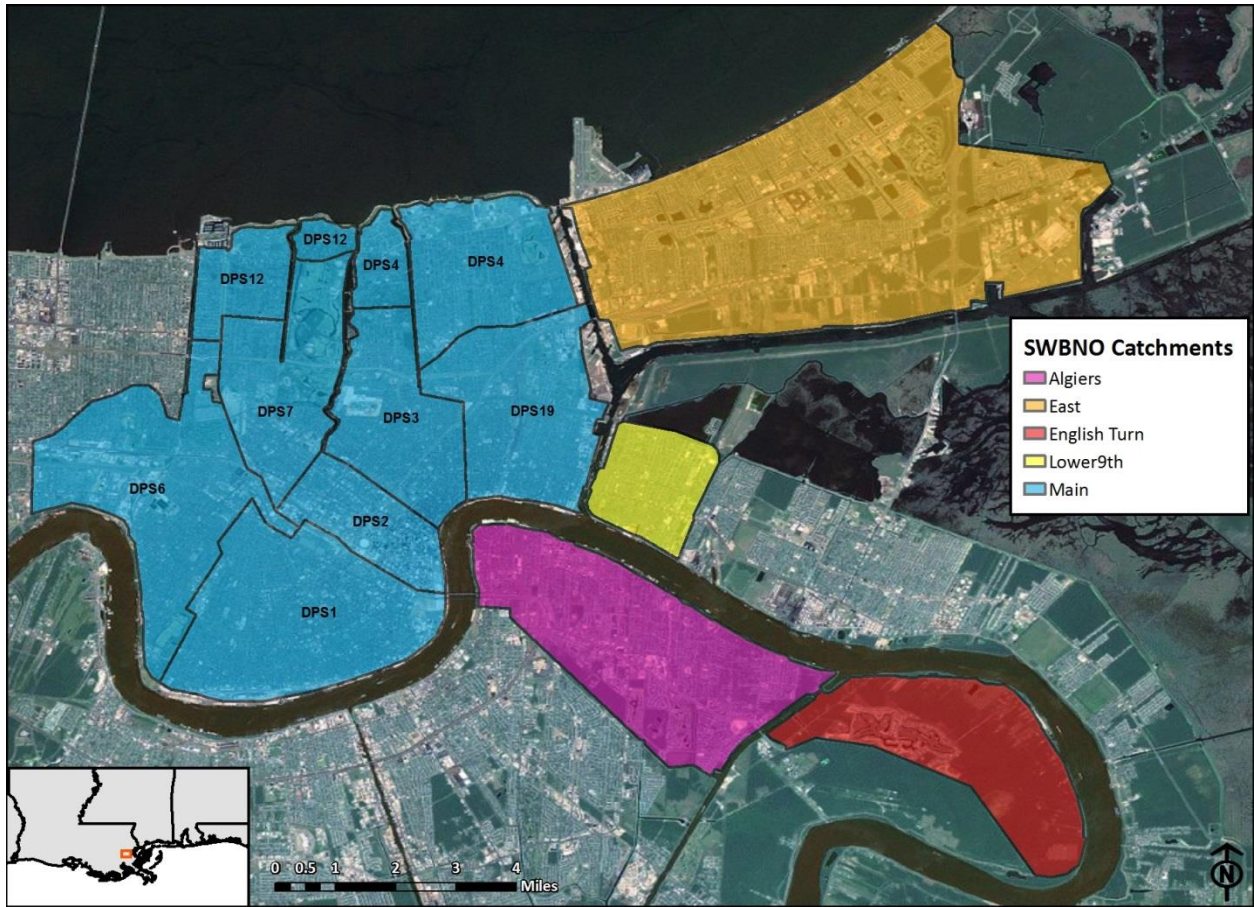
145 *2a. Digitization of SWBNO pumping records*

146 The city of New Orleans can be broken up into five main areas that need to be pumped
147 during rainfall, separated by the Mississippi River, the Inner Harbor Navigation Canal (IHNC),
148 and the Intracoastal Waterway (ICWW). This creates five main polders, or artificial watersheds,
149 within the city, which we have labeled as Main, East, Lower 9th, Algiers, and English Turn
150 (Figure 6). The storm drainage network is independent in each of these areas. To verify rainfall
151 that occurred in the uptown areas of New Orleans, we would only need to estimate the amount of
152 water pumped out of the “Main” polder of the city. This section of the city includes several
153 pumping stations operated by SWBNO: drainage pumping station 1, 2, 3, 4, 6, 7, 12, and 19.
154 Drainage pumping stations 1, 2, and 3 pump from one interior canal to another interior canal, and
155 drainage pumping stations 4, 6, 7, 12, and 19 pump from an interior canal to an outfall canal.
156 Therefore, data from pumping stations 4, 6, 7, 12, and 19 are aggregated to estimate the volume
157 of water pumped out of the city.

158 Hydrologists from the NWS LMRFC contacted SWBNO staff during summer 2013 to
159 request pumping records for New Orleans. SWBNO staff compiled records for the August 26th
160 through August 31st period for stations within the “Main” polder. Records of tailwater,
161 headwater, and whether or not a pump was operating are written on paper log sheets by hand at
162 hourly or half-hourly intervals; an example is illustrated by Figure 7. Hydrologists visited
163 SWBNO offices in September 2013, scanned in over 100 pages of records, and then digitized the
164 records into a spreadsheet. Pumping records from station 12 were not available, however the
165 contributing area to this station was only about 6% of the study area, and was also not impacted
166 by the heaviest rainfall amounts. To accurately estimate the rate of water being pumped by a

167 single pump, the tailwater/headwater elevation difference (static head) is required, as well as
168 relationship between static head and flow rate, which is unique to each pump size and type.

169 After Hurricane Katrina flooded large sections of New Orleans, numerous pump stations
170 were damaged. An Interagency Performance Evaluation Task Force (IPET) was assembled to
171 document the performance of the hurricane protection system in the New Orleans area. In
172 Volume IV of their report, IPET documented the status of the pumping stations and the repairs
173 needed to bring stations back to capacity (Interagency Performance Evaluation Task Force,
174 2006). IPET also created pump curves (plots showing the static head relationship with flow rate)
175 for almost all pumps controlled by SWBNO. Pump curves for 51 different pumps presented in
176 the IPET (2006) report were digitized into a spreadsheet format that could be easily referenced
177 by the pumping records.



178

179 Figure 6. Polders of the New Orleans storm drainage network. The creation of levees to protect
 180 the city of New Orleans from flooding had the side effect of creating several completely-
 181 enclosed, artificial drainage catchments (polders) which must be manually drained. Catchments
 182 within the “Main” polder defined by SWBNO pumping stations are labeled.

183

SEWERAGE & WATER BOARD OF NEW YORK																			
DAILY LOG																			
DRAINAGE PUMPING STATION																			
Time	WATER GAUGES				INDICATING WATT METERS														
	Section		Discharge		6600 V Units					60 Cycle					Vertical Pumps				
	In Back of Screen	In Front of Screen	STPH	ESCO	A	B	C	D	E	F	G	H	I	#1	#2	No.1	No.2	No.3	No.4
12:30	105	105	232	232															
1:00	105	111	233	233															
1:30	105	106	232	232															
2:00	113	119	231	231															
2:30	105	124	233	234															
3:00	113	121	233	233															
3:30	124	121	234	234															
4:00	124	129	233	233															
4:30	126	132	234	234															
5:00	143	151	235	235															
5:30	143	149	235	235															
6:00	143	143	241	240															
6:30	143	144	242	242															
7:00	143	144	243	243															
7:30	149	142	242	242															
8:00	132	139	245	245															
8:30	132	139	244	244															
9:00	132	139	246	246															

184
 185 Figure 7. Example section of a daily log sheet for a pump station operated by SWBNO.
 186

187 *2b. Calculation of runoff from pumping records*

188 Flow pumped by a given pump station was estimated using two different spreadsheets –
 189 one a digitized database of pumping records from Isaac, and another containing a look-up table
 190 derived from digitized pump curves. For a given timestep and pump, if the pump was in
 191 operation, the observed static head was converted to a flow in cubic feet per second (cfs) based
 192 upon the pump curve lookup table, as illustrated by Figure 8. This process was repeated for each
 193 pump in a given pump station for each timestep (either hourly or half-hourly). The pumped flow
 194 rate for each pump was summed by timestep, and then a total pumped volume was calculated.
 195 Dividing the total pumped volume by the contributing area produces EUD, or average runoff
 196 depth.

197

Digitized Pump Record Pump Station 6

G	P	Q	R	AF	AG	AH	AM
Static Head	I on/off	CD1 on/off	CD2 on/off	I cfs	CD1 cfs	CD2 cfs	TOTAL (cfs)
12.1				0	0	0	0
12.8	x			1096	0	0	1096
14.6	x			1026	0	0	1026
14.9		x		0	0	203	203
14.8		x		0	0	203	203
14.6		x		0	0	204	204
14.5		x		0	0	204	204
14.4		x		0	0	205	205
14.4		x		0	0	205	205
14.3		x		0	0	205	205
14.2		x		0	0	205	205
14.3		x		0	0	205	205
14.1		x		0	0	206	206
13.3		x		0	0	208	208
15.6	x	x		980	0	200	1180
15.3		x		0	0	201	201
14.4		x		0	0	205	205
14.3		x		0	0	205	205
14.1		x		0	0	206	206
14.3		x		0	0	205	205
14.4		x		0	0	205	205
15.9	x	x		965	0	199	1164
16.0		x		0	0	199	199

Digitized Pump Curve Pump CD2

	A	B
1	Static Head	Flow (cfs)
2	0.0	620
3	0.1	620
4	0.2	619
5	0.3	619
6	0.4	618
7	0.5	618
8	0.6	617
9	0.7	617
10	0.8	616
11	0.9	616
12	1.0	615
13	1.1	614
14	1.2	613
15	1.3	612
16	1.4	611
17	1.5	610
18	1.6	609
19	1.7	608
20	1.8	607
21	1.9	606
22	2.0	605
149	14.7	204
150	14.8	203
151	14.9	203
152	15.0	203
153	15.1	202

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Figure 8. Flow chart illustrating the estimation of flow from an individual pump at an individual pumping station. The spreadsheet first checks to see if pump is operating (1), if it is not, flow is set to 0 cfs. If the pump is operating, the static head (2) is compared to a lookup table in the digitized pump curve spreadsheet (3) and the corresponding flow (4) is set in the pump record spreadsheet (5) for use in estimating the total flow from each pump for the that timestep (6).

205 *2c. Mitigating sources of uncertainty in pumping records*

206 There are a few concerns with taking the derived flow values from available pumping
207 records that need to be addressed before the data should be used in an analysis.

- 208 1. SWBNO was running some pumps off and on for at least two days prior to the first
209 waves of rainfall impacting New Orleans. This is partly due to attempts to lower interior
210 drainage canals to increase storage capacity of the drainage system.
- 211 2. Although water elevations in the interior drainage canals were fairly constant at times
212 before the onset of rainfall, each canal showed a rising trend after pumping ended prior to
213 the onset of rainfall. This is thought to be due to water in the drainage system from past
214 rain events being able to drain into to the canals after lowering, somewhat similar to
215 baseflow in normal watersheds.
- 216 3. Available SWBNO pumping records ended at 12:00AM CDT September 1st, 2012 but
217 pumping was still ongoing and likely continued after our records ended.

218 To address these concerns, some assumptions and corrections were needed. How we chose to
219 address each issue, specifically:

220 1. **Pumps running off and on prior to Isaac landfall**

221 As mentioned, some pumping prior to landfall of Isaac was likely due to attempts to
222 increase the capacity of the interior drainage canals prior to heavy rainfall, but some may
223 also have been in response to previous rainfall events (August 23rd and August 24th).

224 Because of the inherent lag in a storm drainage system, it would be almost impossible to
225 directly apportion the volume of water from events occurring within a few days of one
226 another. For the purposes of our analysis, we decided that the pumping related to a pre-

227 storm drawdown would have been most likely to occur when forecast tracks for
228 Hurricane Isaac first showed a landfall near southeast Louisiana. As illustrated by Figure
229 9, track forecasts from the National Hurricane Center were quickly moving westward
230 from a Florida panhandle landfall toward the New Orleans area by late on August 26th,
231 and fixated on southeast Louisiana by the morning of August 27th. Thus, we chose
232 11UTC, August 27th, as the cutoff point; water pumped after to this time was attributed to
233 a canal drawdown for Isaac.

234 **2. Canal elevations rising after drawdown during periods of no rainfall**

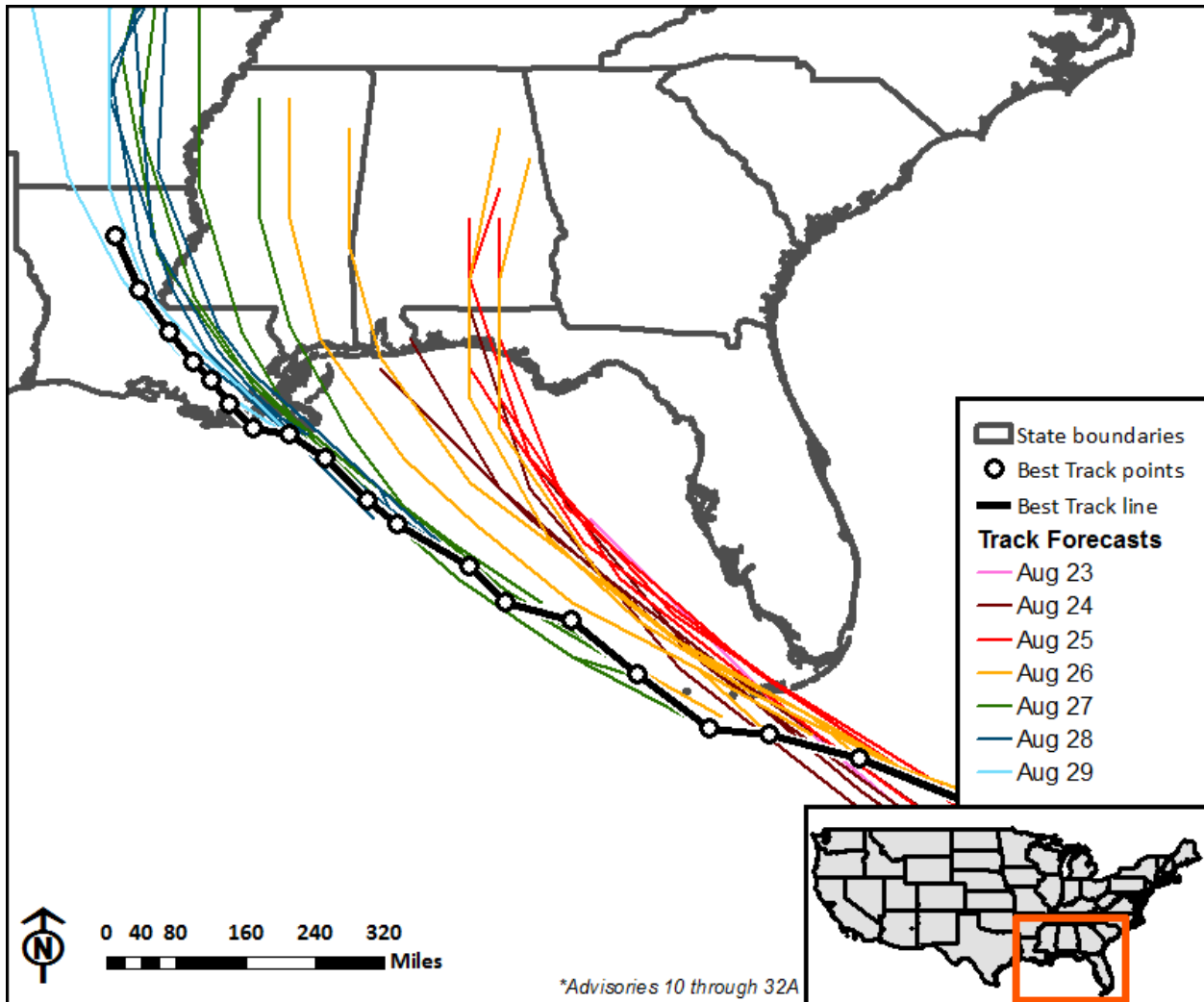
235 It would be almost impossible to determine which sections of the storm drainage network
236 contributed to rising canal levels after brief periods of pumping. For our analysis, we
237 excluded water pumped to draw down the canals – and also pumped to maintain this drop
238 in canal elevations – that occurred before the onset of rainfall, which was roughly 17UTC
239 on August 28th. All water pumped after 17UTC on August 28th was assumed to be from
240 Hurricane Isaac rainfall.

241 **3. Pumping records ending at 12:00AM CDT (5 UTC), September 1st**

242 It was apparent from the data that some additional pumping likely continued after the end
243 of available records and canal elevations had not yet been lowered to pre storm levels.
244 Although we would not necessarily expect canal elevations to return to low levels
245 described in #2 above due to the artificial drawdown, to accurately estimate a volume of
246 runoff from Isaac's rainfall we would need to estimate the volume of additional water
247 that must be pumped to return the canals to that lower, pre-storm level. We estimated a
248 crude elevation-storage relationship for each canal based upon a comparison of pumping
249 to change in elevation during the pre-rainfall period. We acknowledge that there will be

250 some non-trivial uncertainty involved in using this methodology, especially considering
251 that we are unable to account for water in the subsurface drainage network still moving
252 toward the canals.

253



254

255 Figure 9. Five day track forecasts issued by the National Hurricane Center with the preliminary
256 best track for Hurricane Isaac.

257

258 *2d. Improving rainfall estimates*

259 Additional quality control and analysis was done to rainfall estimates in the New Orleans
260 area subsequent to Lincoln, et al. (2013). Some gauges had incorrect meta-data that placed them
261 at the wrong location. Other gauges had bad reports during portions of individual days which
262 necessitated corrections. Several gauges in the New Orleans area still likely under-estimated
263 rainfall due to known measurement biases during windy conditions in tropical storms (Knight &
264 Davis, 2009). The following issues were addressed to produce our final best-estimate rainfall
265 analysis for Hurricane Isaac:

- 266 1. NWS cooperative observer (COOP) weather station NEWL1 was previously shown
267 to be located in the center of Audubon Park, just a bit north of the other COOP station
268 in the area, AUD. We discovered that the location of NEWL1 was incorrect; it was a
269 second rain gauge co-located with site AUD near the Mississippi River, which we had
270 originally treated as a separate gauge. This was also the site associated with the
271 rainfall correction made by NWS WFO LIX staff which we previously concluded was
272 unnecessary, so the 12.0” storm total rainfall amount was also incorrect. We removed
273 this location from our analysis.
- 274 2. Private weather station KLABELLE5, which was originally reported as recording
275 about 17.6” of rainfall, likely recorded higher values but the original data retrieval
276 method did not catch an error in the Weather Underground database. The original
277 retrieval method grabbed daily totals as reported by Weather Underground instead of
278 manually accumulating rainfall rates. This site seemed to report accurate rainfall
279 rates but reported the same value for total rainfall throughout August 29th even before

280 any rainfall. We manually accumulated rainfall rates reported by the site to correct the
281 daily rainfall totals, which yielded a 21.7” storm total rainfall.

282 3. Private weather station KLANEWOR33, which was originally reported to have
283 recorded about 27.4” of rainfall, likely reported erroneous rainfall during a several
284 hour period on August 29th. Because this gauge was the highest known value of
285 rainfall from the storm and had a running gauge accumulation higher than all other
286 gauges, we gave the reading additional scrutiny. Rainfall rates for this gauge and
287 neighboring gauges were compared to radar data at each approximately 5 minute
288 timestep. It was found that all gauges in the area except for KLANEWOR33 matched
289 the radar data closely; increases in rainfall intensity closely matched the passage of a
290 heavier bands of reflectivity associated with the outer edge of Isaac’s eyewall.

291 Rainfall rates for all other gauges were plausible based upon the recorded reflectivity
292 values and associated rain rates determined through the tropical Z-R relationship. It
293 was also noted that there were numerous instances of very high rainfall rates on 5-10
294 minute timescales at the site that did not match neighboring gauges and were not
295 associated with the passage of higher radar reflectivity through the area. One known
296 failure mode for tipping bucket rain gauges to fail in the over-estimate direction can
297 occur during landfalling tropical systems where strong winds cause false tips. This
298 phenomenon seems to be poorly understood and poorly quantified in the peer-
299 reviewed literature even though it seems to be widely known by manufacturers of this
300 type of instrumentation. We found that the time period when rain rates at
301 KLANEWOR33 significantly exceeded neighboring gauge locations correlated
302 closely with the time period when frequent wind gusts above 50mph were reported.

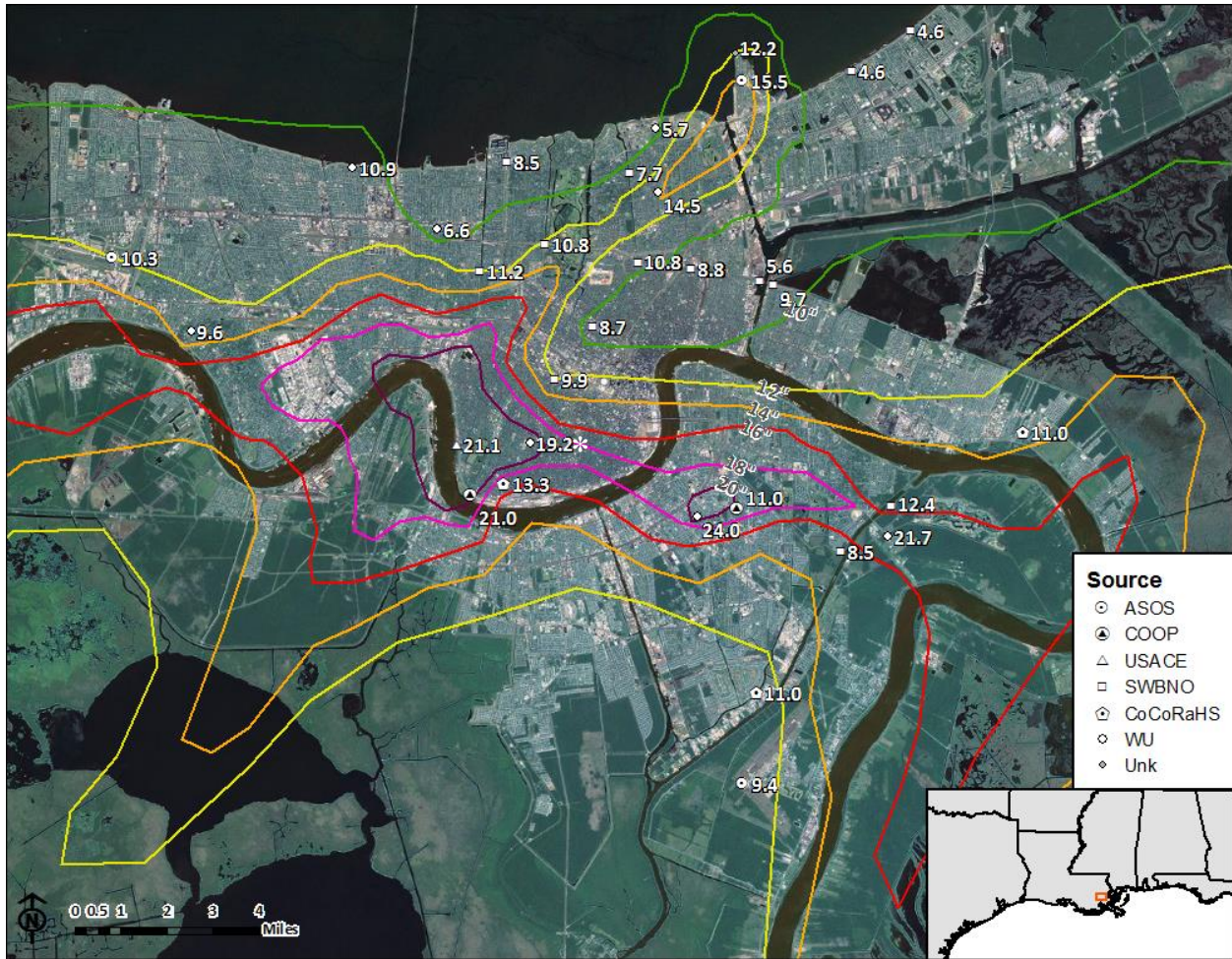
303 Other time periods appeared to report plausible data consistent with neighboring
304 gauges. Because the majority of the data reported by this station appeared to be good
305 and helpful to understanding this rainfall event, we chose to make a correction to the
306 questionable period of time when wind gusts exceeded 50mph. During that period,
307 we forced the rainfall rate for KLANEWOR33 to match the average rate of
308 neighboring gauges (NEWL1, NORL1, KLAGRET4, and KLABELLE5). This
309 adjustment changed the daily total rainfall for August 29th from 24.3 inches to 16.2
310 inches, and thus changed the storm total rainfall from 27.4 inches to 19.2 inches. We
311 acknowledge that this adjustment brings with it considerable uncertainty due to the
312 lack of supporting information by other rain gauge studies.

313 4. NWS COOP weather station TERL1, which recorded 11.0 inches of rainfall, was
314 found to be inconsistent with neighboring gauges along the same swath. Although
315 anecdotal information obtained for Lincoln et al. (2013) suggested that multiple
316 COOP gauging locations besides site AUD may also have experienced failures
317 leading to the under-reporting of storm total rainfall, this gauge was not the same type
318 of reporting station as the sites experiencing the known issues. The equipment used
319 by the observer is an 8 inch rain gauge manually read and reported by an observer
320 who is considered particularly trustworthy (NWS WFO New Orleans staff, personal
321 communication, November 2013). Because no sub-daily data was available,
322 however, we were unable to directly compare rainfall rates from this site to the
323 neighboring Weather Underground location with higher values. Some undercatch
324 may have occurred due to wind effects from Isaac, but the site was not visited and the
325 exact reasoning behind the discrepancy is not clear. The site was not excluded from

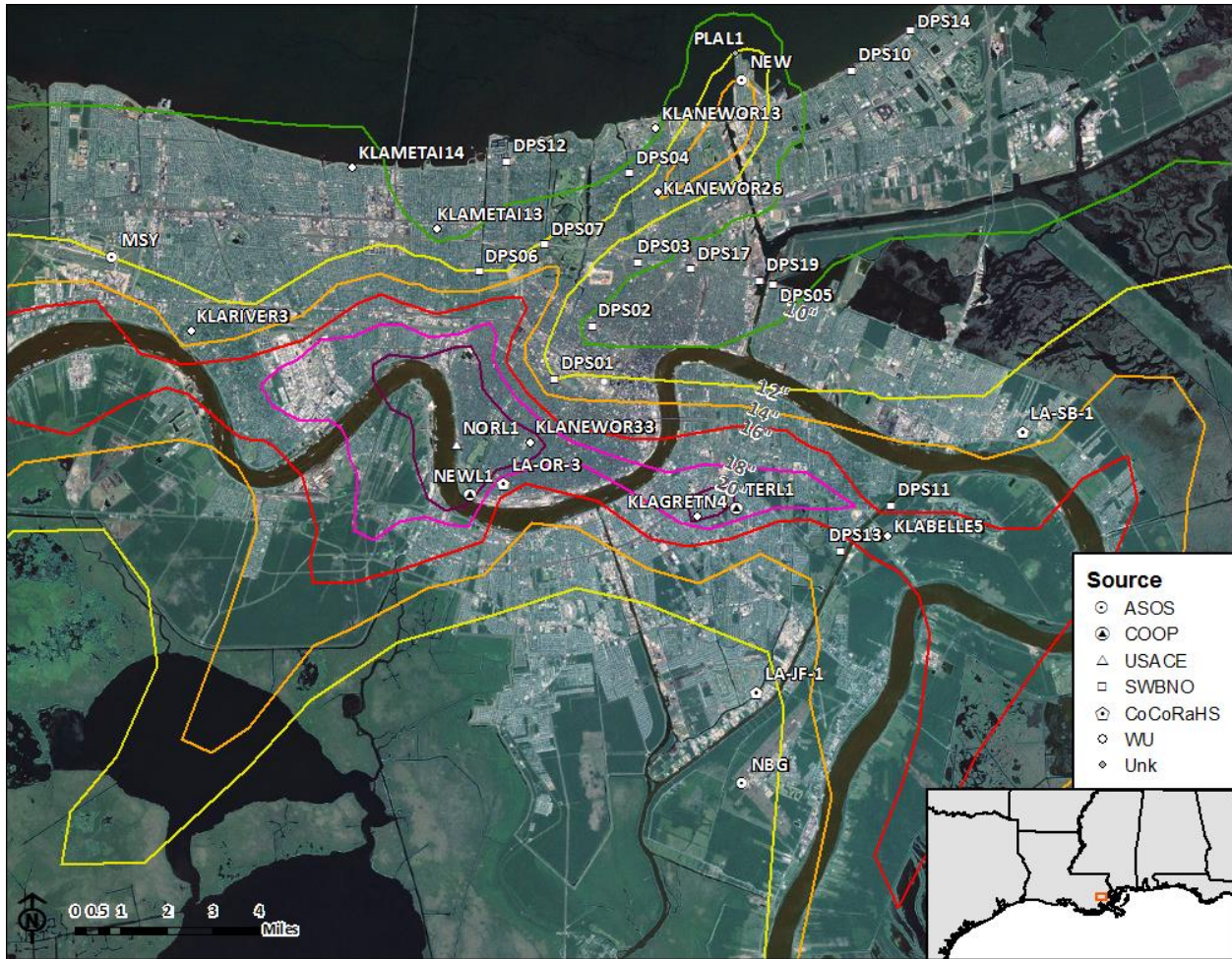
326 analysis but was given low weight in contour analysis when compared to neighboring
327 locations.

328

329 After making these additional corrections to the data it became even clearer that many of
330 the gauge readings from SWBNO were likely under-estimates of actual rainfall. We took this
331 into consideration upon creation of best estimate rainfall analysis map (Figure 10 and Figure 11).
332 In contrast with the earlier analysis presented in Lincoln et al. (2013), the area of highest rainfall
333 has been reduced and many areas of rainfall below 8” have been removed. The swath of rainfall
334 greater than 20 inches has been extended in the east-west direction to match the spatial patterns
335 from radar estimates. The average rainfall for the Main polder changed from approximately 13.7
336 inches to 13.5 inches after adjustments were made. It was also noted that rainfall gauges located
337 in the heaviest swath of rainfall had different timing and magnitude characteristics when
338 compared to rainfall that occurred closer to Lake Pontchartrain (Figure 12, Figure 13, Figure 14).

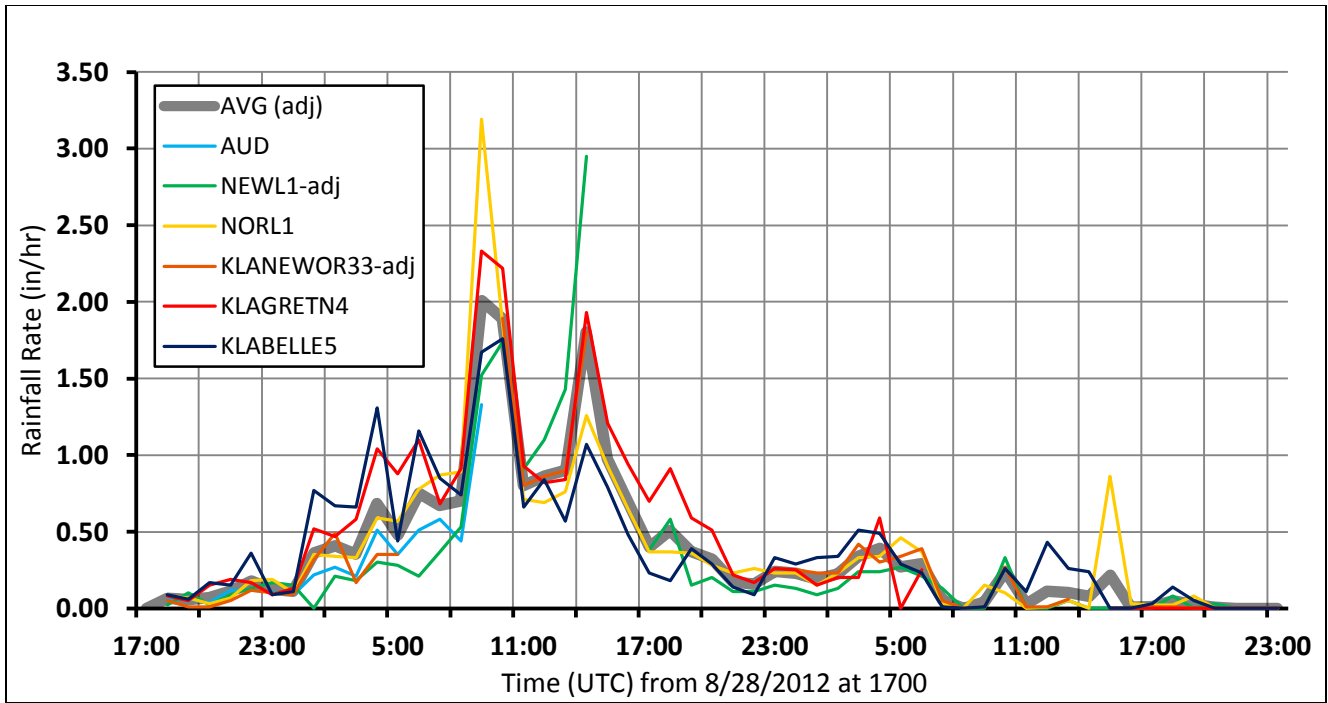


339
 340 Figure 10. Storm total rainfall analyzed from official and private gauges in the New Orleans area
 341 during Hurricane Isaac. Contours were produced from a Kriging interpolation of gauges, then
 342 manually quality controlled to match spatial patterns from radar data and to take into account
 343 likely gauge under-estimates. The value for site KLANEWOR33 (19.2 in) is an estimate; see
 344 discussion for more information.



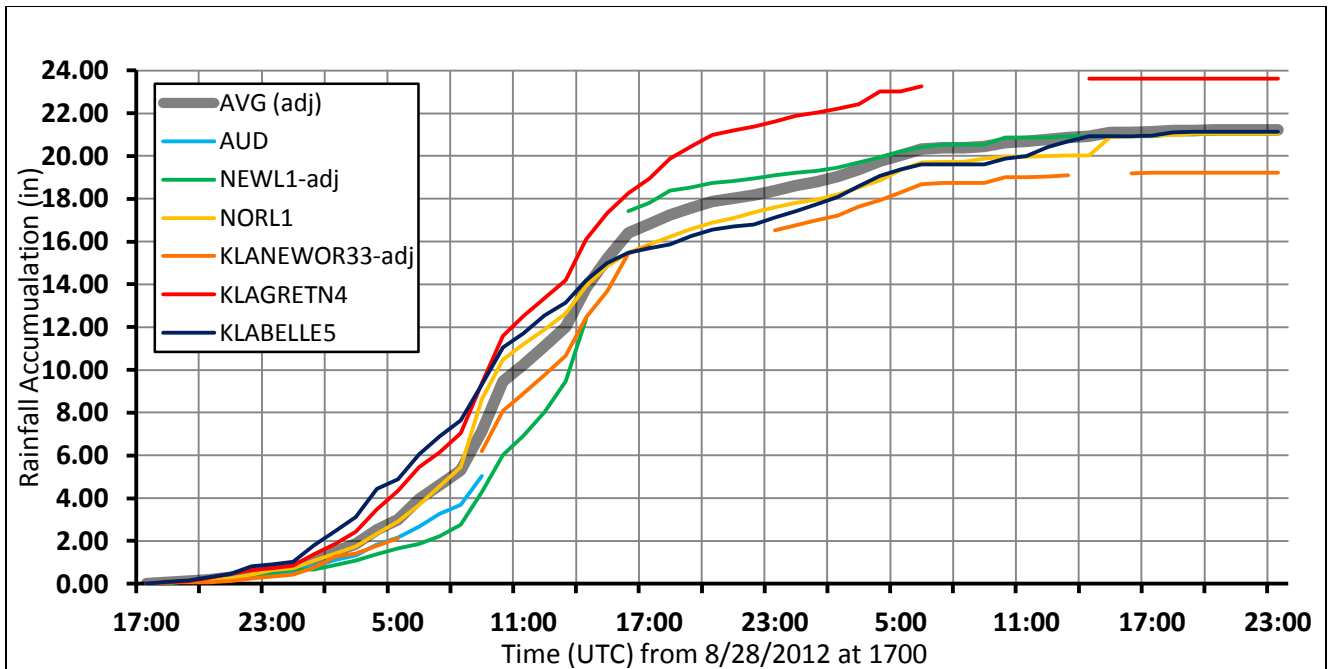
345
 346 Figure 11. Same as Figure 10 but with site identifiers instead of point totals. Sites with four
 347 characters and a number are sites that come in through the HADS network and have an identifier
 348 set by local NWS WFOs. Sites with three characters are ASOS/AWOS airport stations. Sites
 349 starting with “DPS” are SWBNO pumping stations. Sites with eight characters and two numbers
 350 are Weather Underground PWS sites. Sites starting with “LA” followed by two additional
 351 characters and a number are CoCoRaHS sites.

352



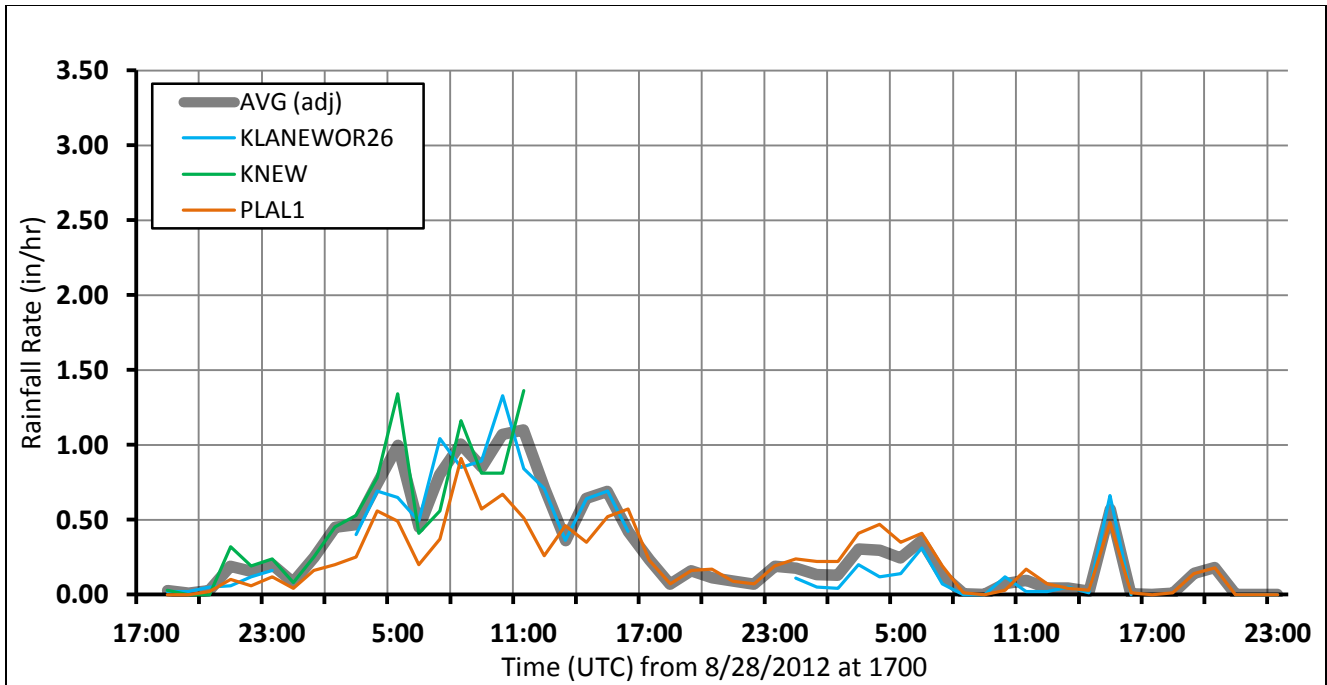
353

354 Figure 12. Hourly rainfall rates for official and private gauging stations in the band of extreme
 355 rainfall near the Mississippi River. Additional quality control steps were applied to the data
 356 since Lincoln et al. (2013) to improve accuracy (see discussion).



357

358 Figure 13. Running rainfall accumulation for the official and private gauging stations in the band
 359 of extreme rainfall near the Mississippi River. Additional quality control steps were applied to
 360 the data since Lincoln et al. (2013) to improve accuracy (see discussion).

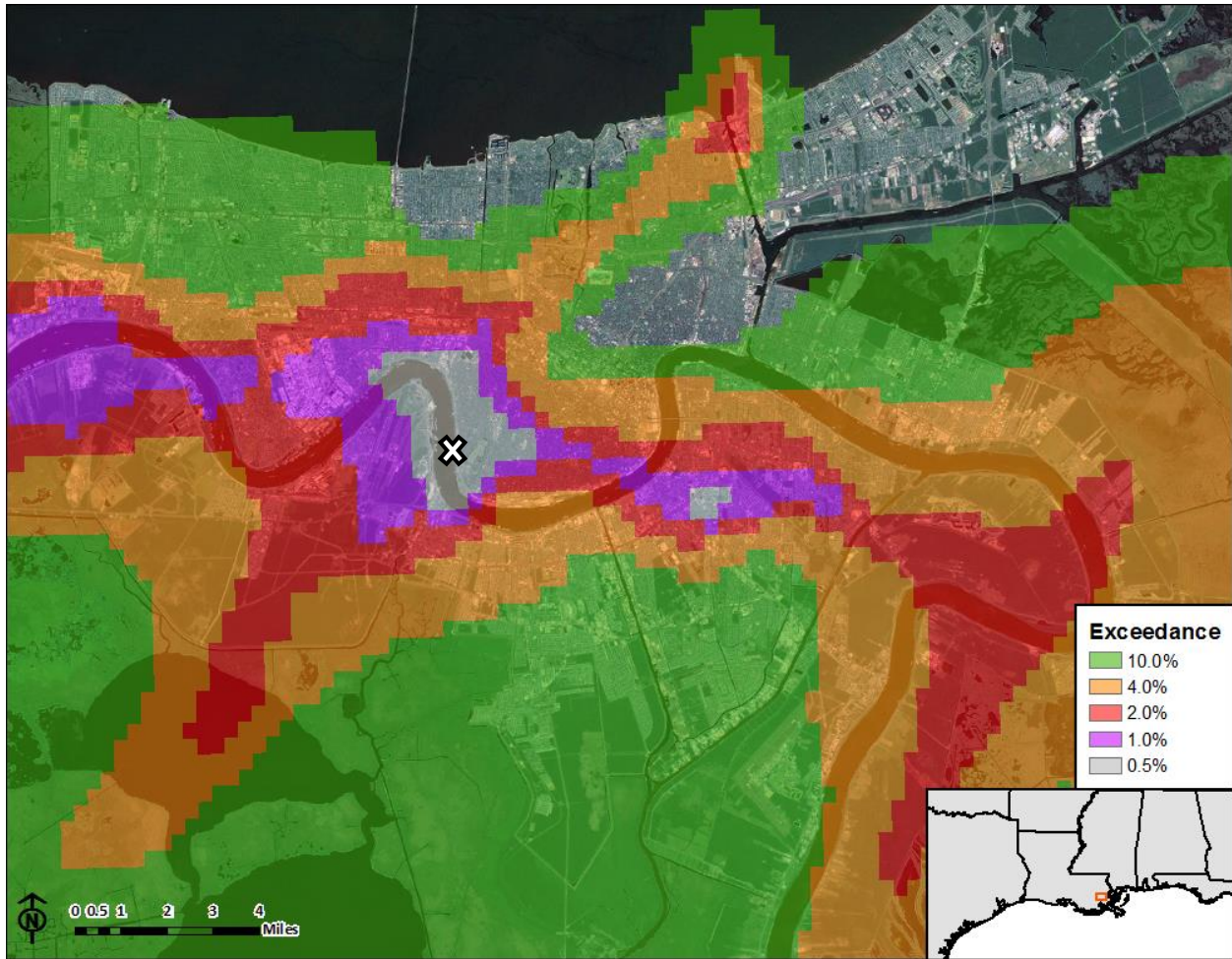


361

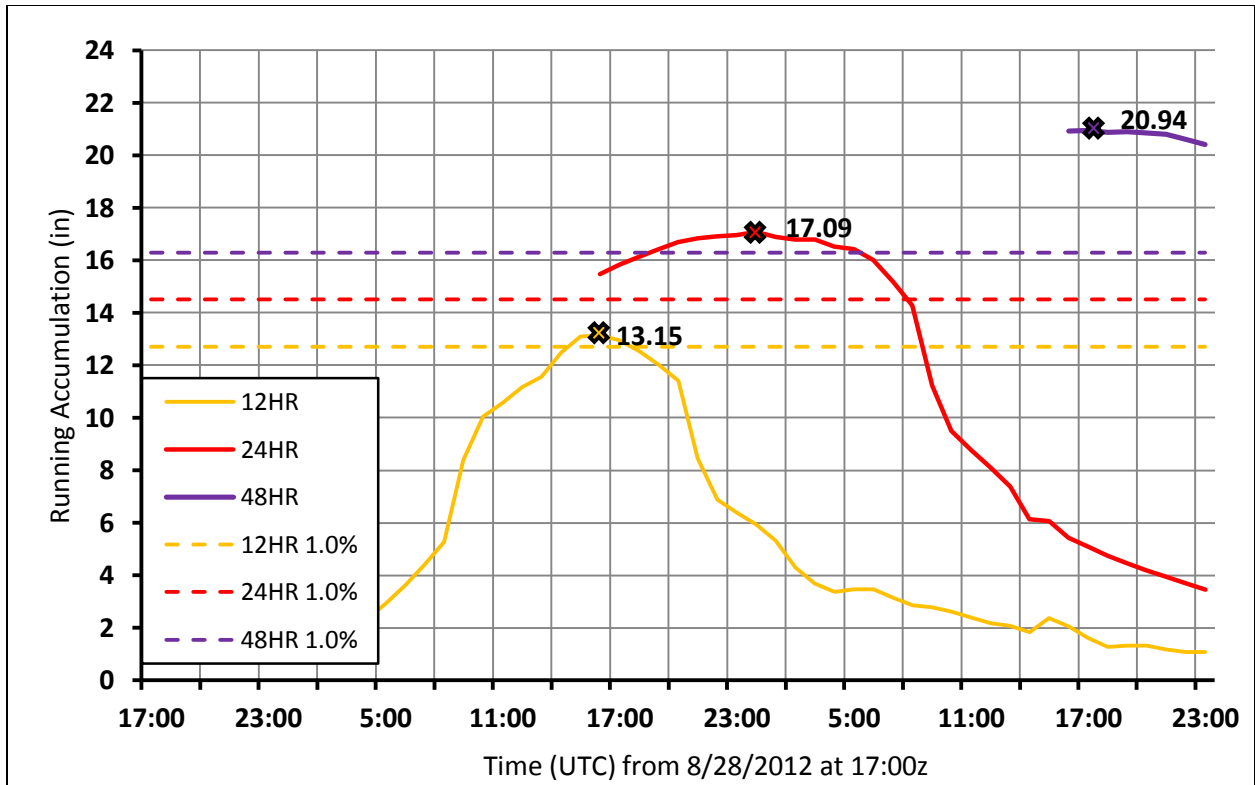
362 Figure 14. Hourly rainfall rates for the official and private gauging stations near Lake
 363 Pontchartrain, just north of the band of extreme rainfall. Additional quality control steps were
 364 applied to the data since Lincoln et al. (2013) to improve accuracy (see discussion).

365

366 The best-estimate rainfall analysis map was compared to published precipitation
 367 frequency estimates in NOAA Atlas 14 (National Weather Service, 2013) to determine the
 368 annual probability of this event occurring in a given year. Rainfall across most of the New
 369 Orleans metropolitan area over the three day period from August 28th to August 30th was
 370 determined to be a 10% annual chance event or greater (greater value is less rare). The heavy
 371 swath of rainfall close to the Mississippi River, however, was considerably more uncommon
 372 with some areas exceeding the 1% annual chance event (Figure 15); for the purposes of our
 373 analysis, we consider rainfall amounts exceeding the 1% annual chance event to be “extreme.”
 374 As with the rainfall data itself, the annual exceedance exhibited a very sharp gradient. Over
 375 shorter durations, rainfall was less extreme (Figure 16), with a running six hour accumulation
 376 barely exceeding the 1% annual chance event in the heaviest swath.



377
 378 Figure 15. Estimated precipitation exceedance for the best-estimate rainfall analysis map (Figure
 379 10) assuming a storm duration of three days. Exceedance values are the estimated chance of a
 380 given rainfall amount occurring in a given year. Extreme rainfall amounts (defined by
 381 exceedance of 1% annual chance event) occurred in an isolated swath near the Mississippi River.
 382 Most portions of the New Orleans metropolitan area experienced less extreme rainfall totals.
 383 The rainfall gauge NORL1 (marked above) is detailed further in Figure 16.



384
 385 Figure 16. Running accumulations for the rainfall gauge NORL1 compared to published
 386 precipitation frequency values. Rainfall amounts become increasingly extreme with longer
 387 durations, suggesting that the storm duration, as opposed to the rainfall intensities, was the
 388 dominant factor in producing the swath of heavy rainfall.

389

390 *2e. Modeling runoff volumes from observed rainfall*

391 We determined that to reconcile rainfall estimates with pumping estimates we needed to
392 create a model to estimate canopy interception, surface abstraction, and infiltration. We chose
393 the freely available Hydrologic Engineer Center (HEC) Hydrologic Modeling System (HMS)
394 developed by the US Army Corps of Engineers to perform this task. The HEC-HMS is not a
395 single model, but a suite of multiple models for multiple steps in the process of producing an
396 outflow hydrograph from provided rainfall data. HEC-HMS has been widely used for event-
397 based modeling and event design storm studies. According to hydrologic theory, we assume that
398 the volume of water pumped out of the city is equal to the average runoff, which can be
399 described by the equation:

400

$$401 P_{excess} = R - A_{canopy} - A_{surface} - I \quad (1)$$

402

403 where P_{excess} is the excess precipitation, or runoff, A_{canopy} is the canopy interception, $A_{surface}$ is the
404 surface abstraction, and I is the infiltration. P_{excess} is estimated from pumping records and R is
405 estimated from rain gauge observations and remotely-sensed radar data, discussed more in
406 Lincoln et al. (2013).

407 We broke the New Orleans Main polder into various subbasins, each defined by a
408 pumping station. The subsurface flow in the storm drainage system is complicated, and in
409 different events water can flow in different directions toward different canals/pumping stations
410 for pumping out of the city. Even with that caveat, modeling multiple basins has the benefit of
411 better-discriminated rainfall variability and land cover characteristics. We made an attempt to
412 delineate local contributing areas for each pumping station based upon: 1) high resolution

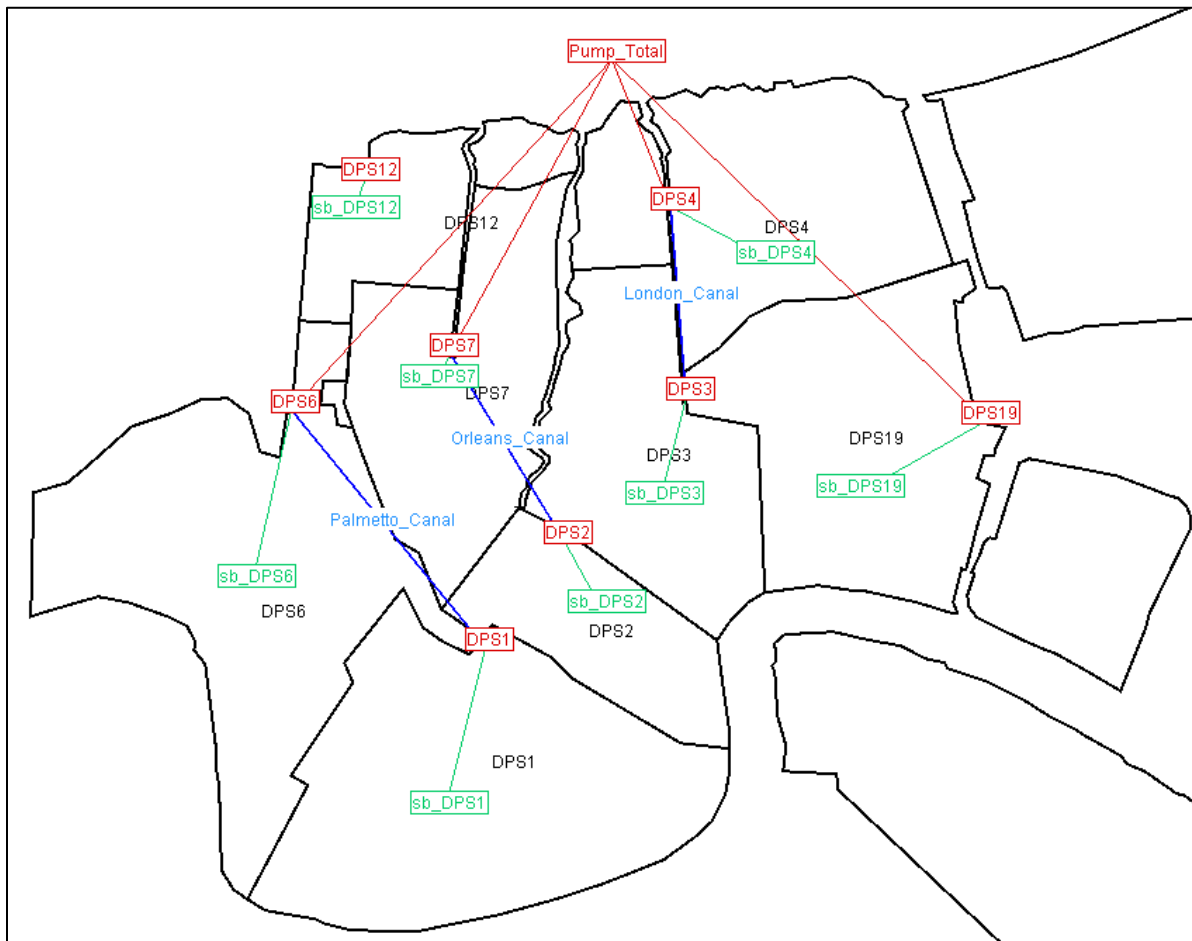
413 elevation data, 2) delineations published in documents from the Gutter to Gulf Initiative
414 (www.guttertogulf.com), and 3) the layout of the storm drainage network provided by the
415 Sewer System Evaluation and Rehabilitation Program (SSERP) website of SWBNO
416 (<http://gosserp.com/>).

417 The resulting HEC-HMS model contains eight (8) subbasins ranging in size from 2.5 to
418 8.2 mi² (Figure 17). Although the pump stations that remove water from the interior drainage
419 network do not pump water into the same canal, we created an artificial confluence downstream
420 of these locations such that we could easily compare modeled volume to observed volume. The
421 model was set to run on a 15-min timestep but we chose to use hourly rainfall data due to the
422 quality-controlled rainfall data available at that interval. Numerous variables were required for
423 the individual modeling methods (US Army Corps of Engineers Hydrologic Engineering Center,
424 2005). Parameters for abstractions (storages of rainfall that must be satisfied before any rainfall
425 interacts with the soil surface) and soil properties needed to be estimated or derived from
426 available datasets. Soil parameters for the central U.S. were previously derived from SSURGO
427 soil survey data in previous collaboration with the National Severe Storms Laboratory (NSSL;
428 Ami Arthur, NSSL, 2012) and were readily available to use in the infiltration method of the
429 model. Abstractions such as canopy interception and surface abstraction, however, are harder to
430 estimate and can vary widely depending type of tree, building, or soil roughness that is blocking
431 the water. In large events, abstractions are very small relative to the total rainfall, which greatly
432 mitigates uncertainty.

433 Canopy interception was modeled with the “Simple Canopy” method, which requires one
434 value representing the subbasin-averaged amount of rainfall that must be retained before rainfall
435 continues to the soil surface. Surface abstraction was modeled with the “Simple Surface”

436 method, which requires one value representing the subbasin-averaged amount of rainfall that
437 must be retained, after falling through the canopy, before rainfall continues to the soil surface.
438 Infiltration was modeled with the Green and Ampt method, a physically-based model of
439 infiltration simplified from the Hortons equation. The Green and Ampt method requires the
440 initial soil moisture, the wetting front suction head (the tension force between the water and the
441 soil), and the saturated hydraulic conductivity (the rate of infiltration once soil is saturated). The
442 parameters used in the model are shown in Table 1.

443



444
445 Figure 17. Schematic of the HEC-HMS model developed for the New Orleans storm drainage
446 network.

447

448 Table 1. Parameters used in the HEC-HMS model developed for the New Orleans storm
 449 drainage network. Although included in the model, modeled flow from pumping station 12 was
 450 ignored in the analysis because pumping records were not available.

Subbasin	Area (mi ²)	Canopy Interception (in)	Surface Abstraction (in)	Sat. Hydraulic Cond. (in/hr)	Wetting Front Suction Head (in)	Impervious (%)
1	8.17	0.10	0.20	0.0573	10.6	56.8%
2	2.67	0.10	0.20	0.0005	12.9	79.3%
3	4.62	0.10	0.20	0.0010	10.2	54.4%
4	5.85	0.30	0.20	0.0006	11.5	39.2%
6	8.22	0.20	0.20	0.0767	13.9	48.7%
7	4.81	0.20	0.20	0.0009	11.7	41.1%
12	2.50	0.30	0.20	0.0005	12.9	36.3%
19	5.92	0.10	0.20	0.0013	11.8	57.5%

451

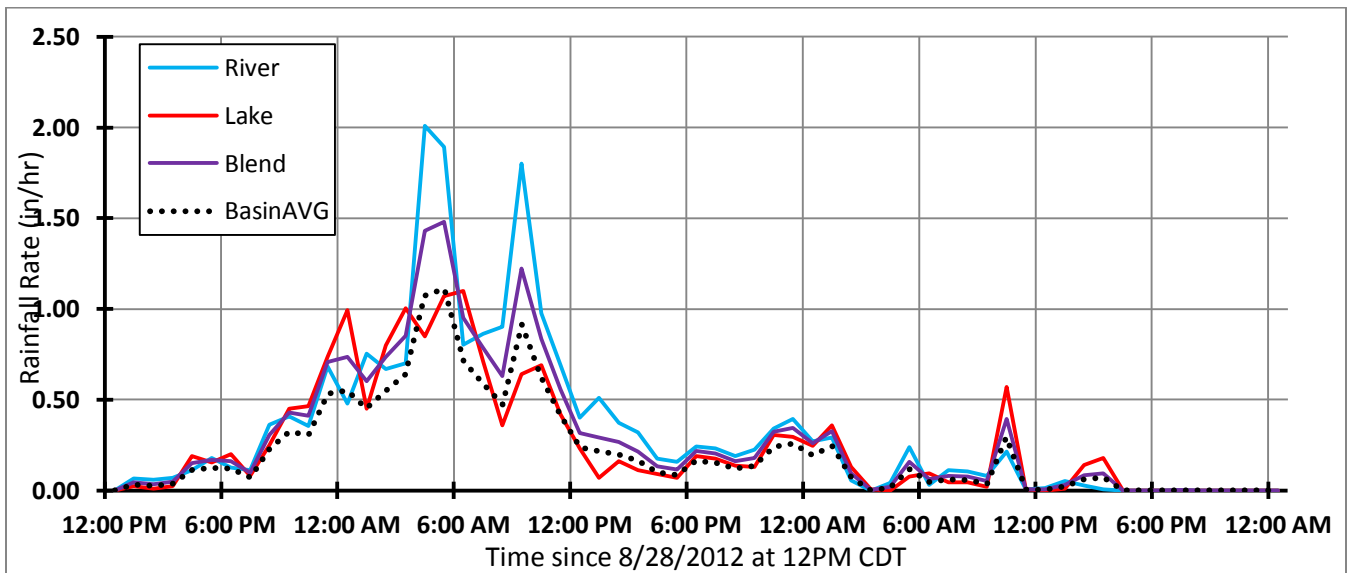
452 Subbasin-average rainfall required by the HEC-HMS model was created from both
 453 individual gauge averages and from the best-estimate rainfall analysis. To account for temporal
 454 variability in the rainfall, hourly rates for gauges within the band of extreme rainfall along the
 455 Mississippi River were averaged to create a “River” rainfall timeseries and hourly rates for
 456 gauges near Lake Pontchartrain were averaged to create the “Lake” rainfall timeseries (Figure
 457 18). The individual stations used to create these rainfall timeseries are shown by Figure 12 and
 458 Figure 14. Model subbasins near Lake Pontchartrain used the “Lake” timeseries and subbasins
 459 near the Mississippi River used the “River” timeseries. The rainfall values in both timeseries
 460 were weighted to match the subbasin average of the event total produced from the best-estimate
 461 storm total rainfall analysis (Table 2).

462

463 Table 2. Storm total rainfall for each model subbasin derived from the best-estimate storm total
 464 rainfall analysis.

Subbasin	Average Rainfall (in)
1	16.97
2	11.29
3	10.42
4	12.02
6	17.35
7	12.28
12	9.11
19	9.50

465



466
 467 Figure 18. Rainfall timeseries data used to drive the HEC-HMS model. The character of the
 468 rainfall differed between areas near Lake Pontchartrain and areas near the Mississippi River.
 469 The individual hourly ordinates were weighted for each subbasin of the Main polder depending
 470 upon the subbasin-averaged value from the best-estimate storm total rainfall analysis (Figure 10
 471 and Table 2). Hourly rainfall averaged across the entire Main polder (and weighted to match the
 472 best-estimate storm total) is displayed as “BasinAVG.”

473

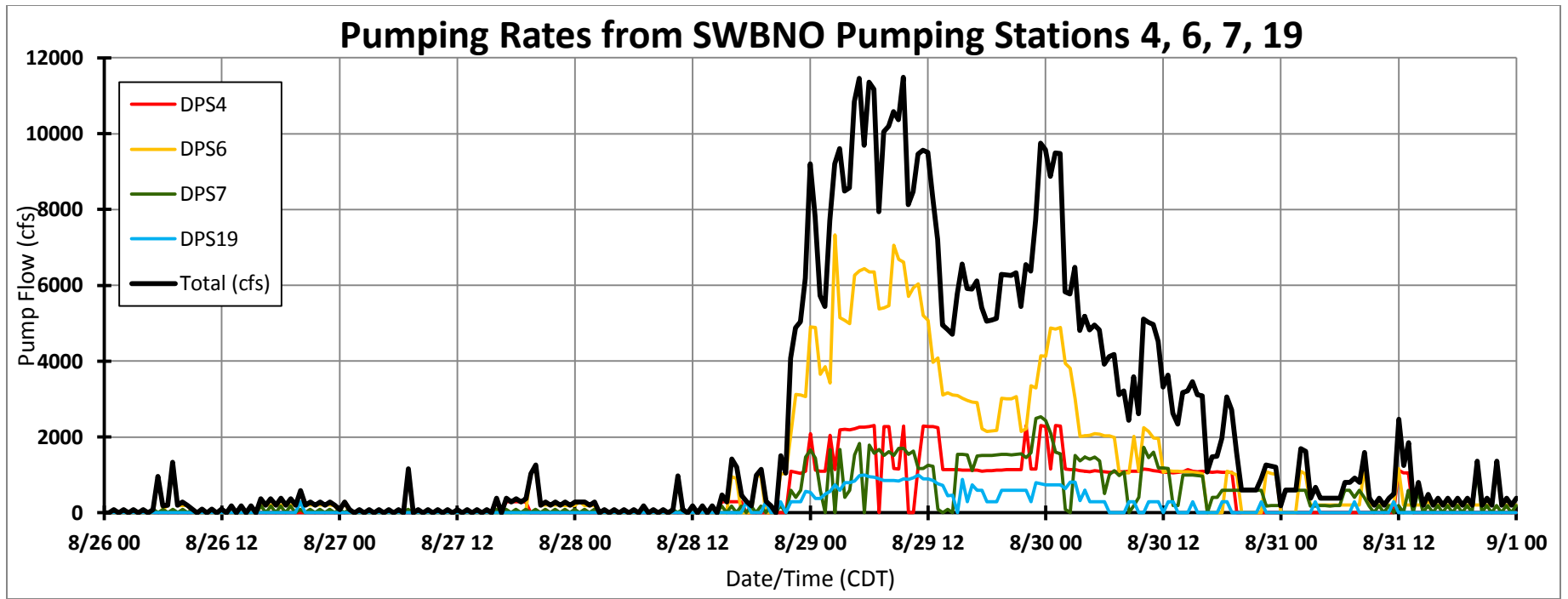
474 **3. Results and Discussion**

475 *3a. Pumping records*

476 The rate of water pumped from each pump servicing the Main polder of New Orleans
477 was calculated from pump curves, and then summarized by pumping station. Pumping rates are
478 illustrated by Figure 19. As mentioned in *2c. Mitigating sources of uncertainty in pumping*
479 *records*, some water pumped prior to the onset of rainfall should be excluded because it was
480 likely due to prior rainfall; this data is not excluded from the figure. It was also necessary to
481 account for ongoing pumping at the end of the period of record, as previously discussed. The
482 EUD of water pumped from the Main polder of New Orleans during Hurricane Isaac was
483 estimated to be 12.13 inches and 11.94 inches, before and after these adjustments were applied to
484 the data, respectively. The 11.94 inch value should be approximately the same as the runoff
485 from the storm after canopy interception, surface abstractions, and infiltration are subtracted
486 from rainfall.

487 As a by-product of the pumping record analysis, we also calculated hypothetical
488 maximum pumping rates for the New Orleans drainage network. Pumps have the greatest
489 capacity when the static head is zero, so this situation was used to estimate the maximum
490 possible pumping rate for the system if all pumps were operating simultaneously. Determining
491 the minimum pumping rate when all pumps are in operation simultaneously is somewhat more
492 complicated because pumping capacities would approach zero as static head increases. We used
493 the maximum static head value presented in the pump curves to calculate the minimum rate.
494 Pumping rates provided by SWBNO, referred to as the “nominal” pumping rates, fell between
495 our calculated minimum and maximum. The estimated minimum, nominal, and maximum
496 pumping rates for the New Orleans drainage network were approximately 12,990 cfs, 19,810 cfs,
33

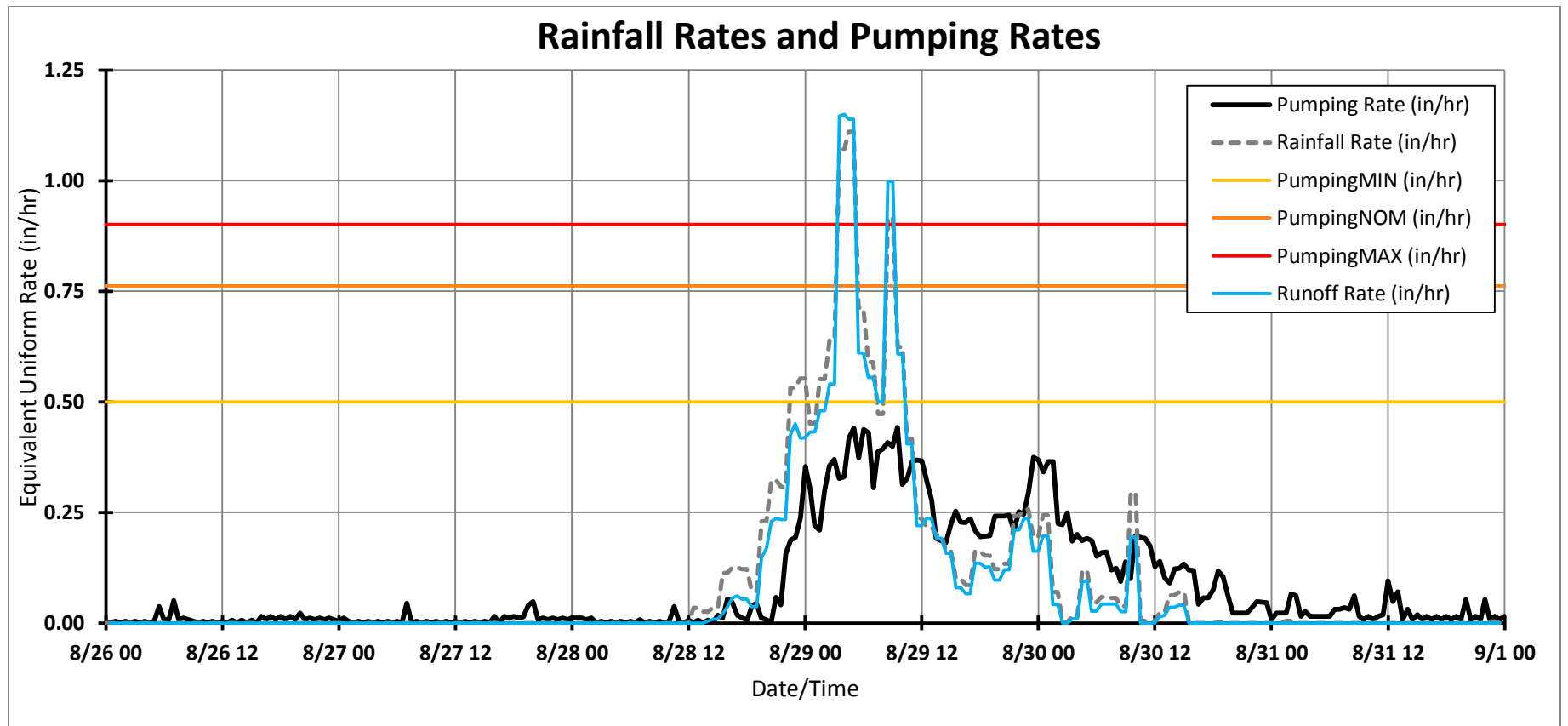
497 and 23,410 cfs, respectively. The equivalent uniform rates for the minimum, nominal, and
498 maximum pumping rates were 0.50 inches/hour, 0.76 inches/hour, and 0.90 inches/hour,
499 respectively. Rainfall rates and pumping rates estimated during Hurricane Isaac for the Main
500 polder of New Orleans are illustrated by Figure 20.



501

502 Figure 19. Estimated pumping rates by pumping stations draining the Main polder in New Orleans during Hurricane Isaac.

503



504

505 Figure 20. Rainfall and pumping rates for the Main polder of the City of New Orleans during Hurricane Isaac. The hypothetical minimum
 506 and maximum pumping rates for the system are specified, as well as the nominal rate provided by SWBNO.

507 *3b. Modeling results*

508 Although we set up the HEC-HMS model with numerous subbasins to better capture
509 rainfall variability, the total modeled runoff from all four exterior pumps (4, 6, 7, and 19) with
510 observed pumping data is assumed to be the best comparison to storm total runoff due to the
511 complexity of the drainage network. To quantify the amount of water lost to canopy
512 interception, surface abstraction, and infiltration (referred to as “loss” in the model), we exported
513 modeled timeseries data from each subbasin, and then computed a weighted average for each
514 timestep to represent the polder-wide value. Modeled rainfall loss ranged from 1.5% (0.17
515 inches) in the subbasin covering the Central Business District neighborhood to 20.4% (3.54
516 inches) in the subbasin covering the Uptown neighborhood. Averaged across the entire Main
517 polder, our model indicated 10.2% (1.39 inches) of loss out of 13.54 inches of rainfall, yielding
518 12.13 inches of runoff. As expected, modeled runoff and estimated pumping for individual
519 subbasins had much more variability than the polder average (Table 3).

520 For roughly the first half of the rainfall event, runoff rates estimated by the HEC-HMS
521 model exceeded the estimated pumping rates for the Main polder of New Orleans. During times
522 when the runoff rate exceeded the pumping rate, storm water could conceptually be considered
523 “in storage.” The rate of storage accumulation was fastest between roughly 2:00AM and
524 9:00AM CDT on August 29th, reaching about 4.0 inches of equivalent uniform depth before
525 pumping rates began exceeding runoff rates and storage started to fall. To determine how much
526 of this “stored” runoff could have been moving through the drainage network, we attempted to
527 estimate the capacity of the network using GIS methods. We digitized the main canals and box
528 culverts of the system as defined by the SSERP website of SWBNO, using specified widths and
529 heights when available and estimating when unavailable. We estimated that the maximum

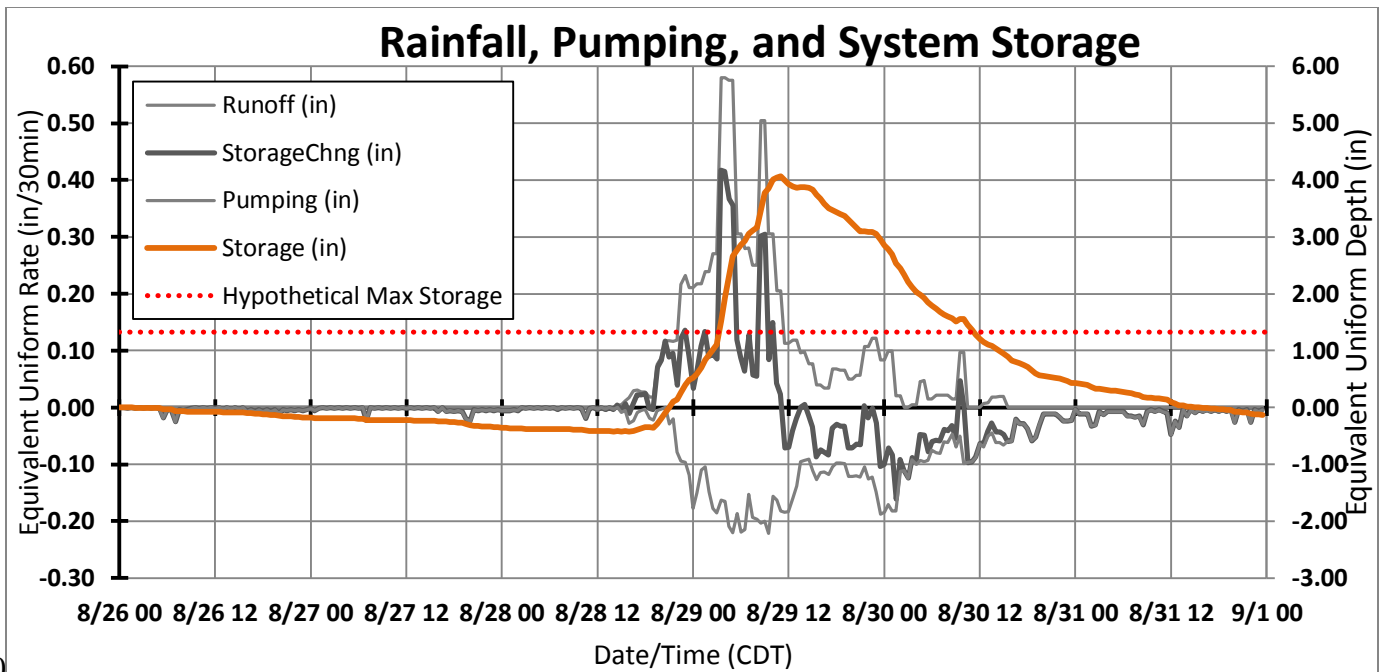
530 potential storage of the storm drainage system is approximately 1.3 inches, however the effective
 531 storage is likely considerably lower and would be very difficult to quantify. This suggests that
 532 over a 36-42 hour period (1:00AM CDT August 29th through 3:00PM CDT August 30th) more
 533 water was likely stored, or moving through, the drainage system than could hypothetically be
 534 stored by it (Figure 21). We hypothesize that this value is not a discrepancy, but instead is an
 535 approximation of the average depth of overland flow in yards and streets during the height of the
 536 storm.

537

538 Table 3. Summary of results from the HEC-HMS model of New Orleans for Hurricane Isaac.

Subbasin	Rainfall (in)	Loss (%)	Loss (in)	Modeled Runoff (in)
1	16.97	13.5%	2.29	14.77
2	11.29	1.5%	0.17	11.02
3	10.42	2.2%	0.22	10.11
4	12.02	4.3%	0.51	11.43
6	17.35	20.4%	3.54	13.88
7	12.28	3.3%	0.40	11.76
19	9.11	2.7%	0.24	8.77
PolderAVG	13.54	10.2%	1.39	12.13

539



540
 541 Figure 21. Runoff, pumping, and net change in system storage at each 30 minute timestep. The
 542 running accumulation of system storage (relative to August 26th at 12:00 AM) is also plotted to
 543 show times that SWBNO pumps are “ahead” or “behind” the accumulated runoff. Hypothetical
 544 system storage represents the maximum possible volume of water that could be held by the
 545 drainage network

546 *3c. Discussion*

547 There are several sources of uncertainty in our analysis that must be recognized before
548 our results can be discussed. Sources of uncertainty include the digitizing of pumping records,
549 the estimation of pump curves, analysis of rainfall, and estimation of parameters for the
550 modeling of runoff. When possible, we attempted to quantify the potential error from incorrect
551 input data to our analysis, expressed as an equivalent uniform depth, or runoff, across the Main
552 polder.

553 Because pumping records from SWBNO are done by hand on paper log sheets, digitizing
554 the information required reading different handwriting styles. We also found that there was not a
555 uniform method for logging the tailwater and headwater elevations that would actually be
556 relevant to the operation of the pumps at each pumping station; some stations also logged the
557 water elevation recorded at the debris screens which did not always match elevations closer to
558 the pumps, but the same log sheet column was not always used to specify which measurement
559 was from which location. During some periods, pumping records were taken every hour, even
560 when pumps were in operation, leading to some confusion on whether the pumps were
561 continuously operating or were running for only brief, intermittent periods. To mitigate these
562 concerns with digitizing the pump records, deductive reasoning was used, as well as consensus
563 opinion of several individuals. Entering incorrect information for headwater and tailwater
564 elevations for a single pumping station during periods of highest pumping usage could
565 potentially change the polder-averaged runoff value by 0.01-0.02 inches for each 30 minute
566 timestep that is in significant error. Erroneously indicating one of the largest pumps (1000 cfs
567 capacity or greater) as in operation could potentially change the polder-averaged runoff value by
568 0.01-0.02 inches for each 30 minute timestep in error.

569 As discussed earlier, some assumptions and corrections were necessary to use the
570 pumping data from SWBNO. Although we expect that the adjustments improved the data
571 analysis, some non-trivial uncertainty may have been introduced that is difficult to quantify. The
572 greatest uncertainty was likely introduced from the lack of pumping data after 12:00AM CDT on
573 Sept 1st. Pumping, average roughly 250 cfs at the end of the record, continued for an unknown
574 amount of time. We roughly approximate that for each 30 minute timestep, a 1000 cfs error
575 would correlate to roughly 0.01-0.02 inches of polder-averaged runoff, based upon uncertainties
576 described previously.

577 Pump curves for the SWBNO drainage network were digitized from the IPET report
578 (2006). Some of these pump curves were created from engineering specifications available from
579 the pump manufacturers. Some pump curves were estimated from hydraulic modeling software.
580 When little information was available on a particular pump, the IPET report did not create a
581 pump curve. When no pump curves were available from the report but the digitized pumping
582 records necessitate a pump curve to estimate runoff, we used the nominal value reported by
583 SWBNO and applied that flow to the entire range of static head values. It would be very
584 difficult to quantify the error in polder-averaged runoff due to an incorrect pump curve because
585 of widely-varying pump capacities. We roughly approximate that for each 30 minute timestep, a
586 1000 cfs error would correlate to roughly 0.01-0.02 inches of polder-averaged runoff, based upon
587 uncertainties described previously. Because we were not involved in the creation of these
588 relationships, however, it is hard to fully quantify potential uncertainty.

589 Due to the subjective nature of contour analysis, there will be some hard-to-quantify
590 uncertainty introduced from the rainfall estimates. We believe that rainfall estimates were
591 improved since Lincoln et al. (2013) after additional gauges were corrected. The volume of
41

592 rainfall was higher than the volume of water pumped out of the Main polder of New Orleans, as
593 expected. The volume of rainfall also closely matched results of modeling analysis which we
594 used to estimate losses from abstractions and infiltration. Similar values reported by nearby
595 gauges for hourly rainfall rates and total rainfall accumulations also increases our confidence in
596 our analysis.

597 The use of a hydrologic model was necessary to estimate losses from abstractions and
598 infiltration and thus calculate runoff from rainfall. This hydrologic model may also have
599 introduced some uncertainty to our analysis. The parameters for the infiltration portion of the
600 model (Green & Ampt equation) were derived from high resolution soil surveys and published
601 values for soil properties, but were not calibrated. The most-sensitive parameter to the Green &
602 Ampt equation is saturated hydraulic conductivity, which approximates the rate of infiltration
603 after the onset of rainfall when the soil surface is saturated. For the city of New Orleans,
604 saturated hydraulic conductivity values were very low due to high clay content and soil
605 compaction through urbanization. In some sections of the city, the values were at the low end of
606 the range allowed by HEC-HMS (just above zero); as such, uncertainty due to the model would
607 mostly be estimated by increasing hydraulic conductivity values. We first set hydraulic
608 conductivity to the lowest allowable value for each subbasin of the polder, which yielded a
609 change in modeled runoff of +1.05in, or +8.8%. Next we changed the hydraulic conductivity for
610 each subbasin by -10%, +10%, +50%, and +100%, which yielded a change in modeled runoff of
611 +0.07in (+0.6%), -0.06in (-0.5%), -0.30in (-2.5%), and -0.56in (-4.7%), respectively. Very large
612 errors in the estimated model parameters are necessary to cause even modest errors in the
613 modeled runoff.

614 After relevant adjustments were applied to rain gauges, storm total rainfall amounts from
615 Hurricane Isaac were very consistent both spatially and temporally in a narrow swath along the
616 Mississippi River that was once considered questionable. Modeled runoff volumes from the
617 HEC-HMS model for the entire Main polder (12.06 inches) were very close to calculated runoff
618 volumes as estimated via pumping records from SWBNO (11.94 inches); the HEC-HMS model
619 over-estimated the runoff by only 1% when compared to the pumping-derived runoff. These
620 results give us high confidence that the isolated rainfall maximum of greater than 20 inches did,
621 in fact, occur across portions of New Orleans near the Mississippi River during Hurricane Isaac.
622 Analysis of sources of uncertainty suggest that very frequent and/or large errors in input data
623 would be required to yield substantial error in our analysis results.

625 **5. Conclusions**
626

627 We continued efforts started in Lincoln et al. (2013) to verify an isolated band of extreme
628 rainfall over portions of New Orleans during Hurricane Isaac. First we summarized New
629 Orleans hydrology and described the impact of Isaac on the city. Then we presented a
630 methodology for estimating the EUD (runoff) from SWBNO pumping records. We also
631 described efforts to further improve our estimates of rainfall to compare to pumping. Next we
632 presented a HEC-HMS model that was used to estimate runoff and losses from the rainfall. We
633 found that the modeled runoff (12.13 inches) very closely matched the runoff estimated from the
634 pumping records (11.94 inches). From this we conclude that there is strong evidence that the
635 isolated, extreme rainfall maximum did occur in sections of New Orleans near the Mississippi
636 River, and despite several inches of runoff going into storage somewhere in the drainage network
637 or on the land surface, no significant flooding was reported.

638 As noted several times through our studies of rainfall of Hurricane Isaac, gauges can be
639 problematic for realtime rainfall applications. Gauges are prone to under-catch during landfall of
640 tropical systems, and in the case of private stations, gauges may also suffer from power and/or
641 data failure. Bands of heavy rainfall like the one analyzed from Isaac are also small enough that
642 they could conceivably pass between gauges, undetected. NEXRAD radar data is presumed to
643 mitigate this concern because it can provide estimates between gauging locations. As noted in
644 Lincoln et al. (2013), however, these radar estimates substantially underestimated rainfall where
645 the extreme rainfall totals occurred, while over-estimating rainfall in most other locations. This
646 finding suggests that future work should entail better discrimination of warm-rain-dominated
647 precipitation bands and consideration of additional radar-rainfall relationships.

648 **6. Acknowledgements**

649 The authors would like to acknowledge Dr. Jeff Masters and Shaun Tanner from
650 WeatherUnderground for helping us obtain private weather station data. Daryl Herzmann and
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652 the source for processed NMQ/Q2 radar precipitation data and daily NWS COOP observer
653 reports. Ami Arthur from the National Severe Storms Laboratory should be acknowledged for
654 her efforts to estimate soil parameters from high resolution soil survey data. The authors would
655 also like to acknowledge the New Orleans Sewerage and Water Board for providing us access to
656 the pumping records as well as their daily rainfall data.

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